



**UNIVERSITÉ  
DE GENÈVE**

FACULTY OF SCIENCE  
Department of Astronomy



Les Gustins Summer School 2024

# Exoclimate Modelling:

## Investigating the Effect of Dynamics on Climate with an Energy Balance Model

Marine Leyvraz

19.07.2024



**Supervisors:** Siddharth Bhatnagar, Emeline Bolmont, Maura Brunetti, Jérôme Kasparian & Alexandre Revol

# Structure

## 1. Introduction

Habitable zone

TRAPPIST-1

Tides

## 2. Methods

N-body code

Climate model

## 3. Model validation

Insolation

Diffusion coefficient

## 4. Results

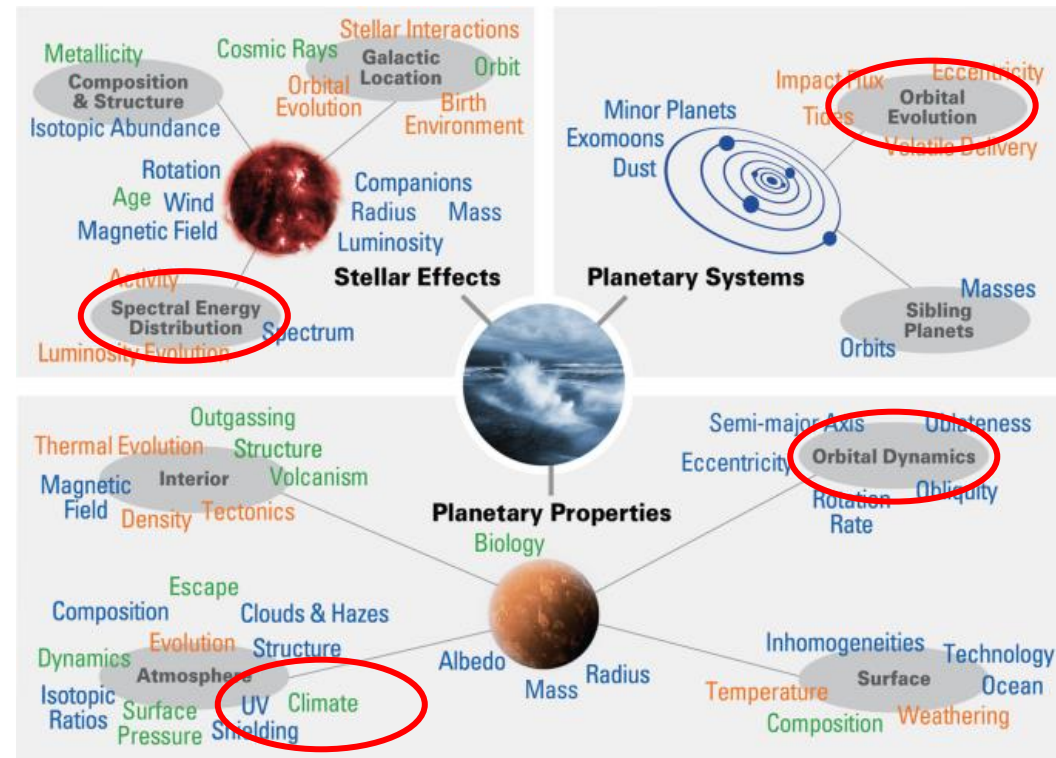


# Habitable zone planets

**Habitable zone**  
*Range of orbital separations around a star within which liquid water could be sustained on the surface of a planetary body.*

Huang, 1959; Kasting et al., 1993

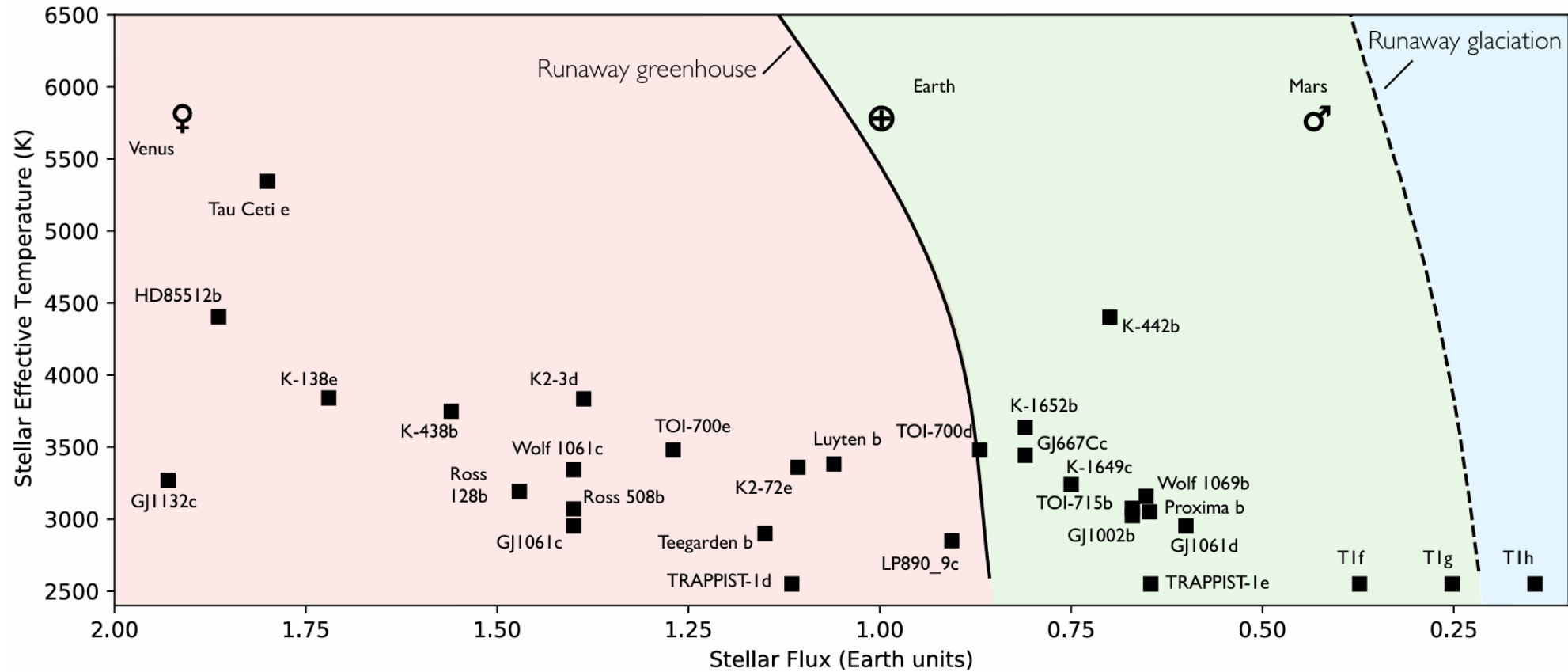
Many elements have an impact on the habitable zone...



Meadows & Barnes, 2018

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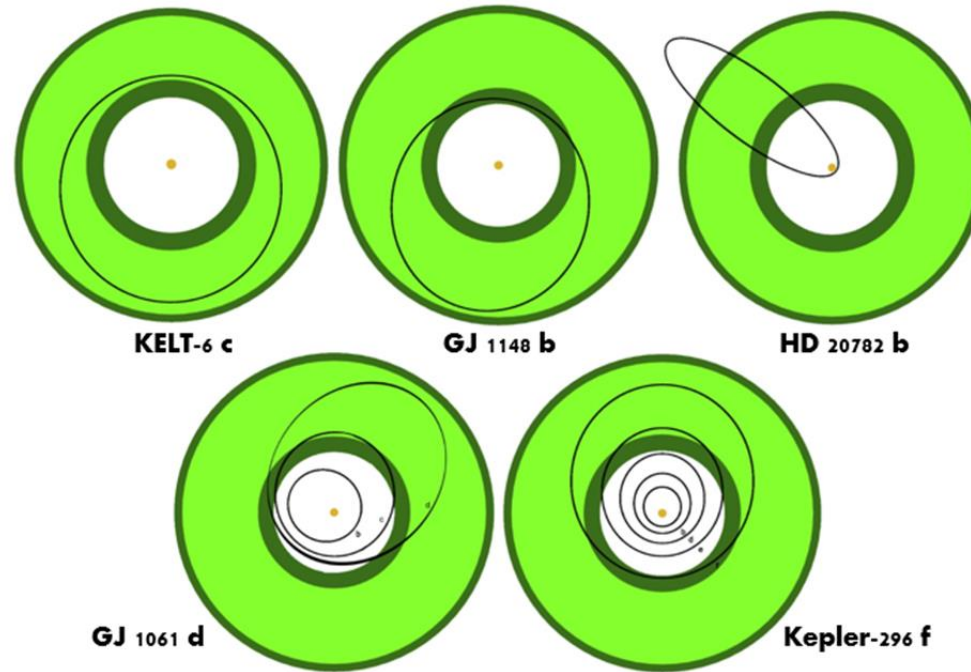
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**Habitable zone planets**



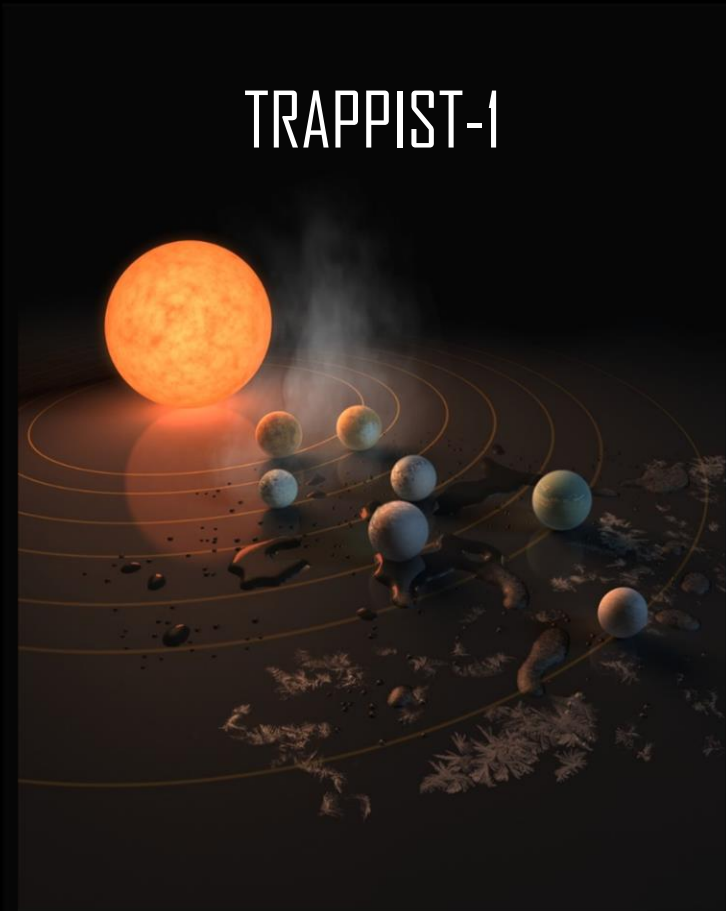
**Permanent surface liquid water**



Hill et al. 2023



# TRAPPIST-1 system



Credit: NASA/JPL-Caltech/R. Hurt (IPAC)

**7 rocky planets**

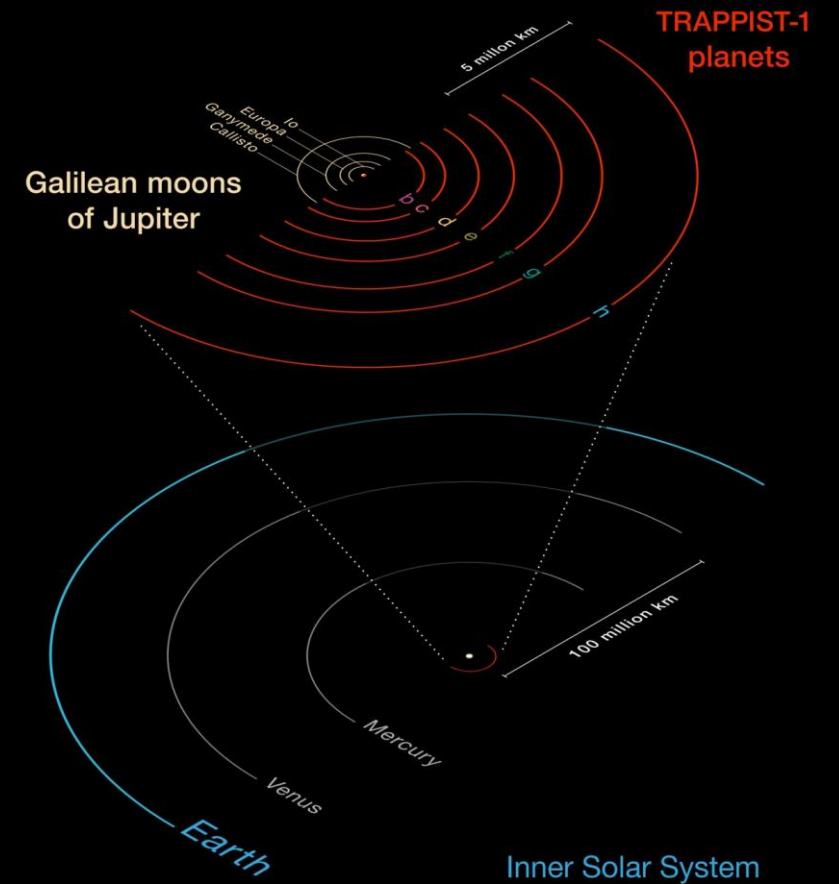
**3 planets in habitable zone**

**M-dwarf host star**

**Compact system**

## Orbit Comparison

between TRAPPIST-1 planets, Galilean moons of Jupiter and inner Solar System



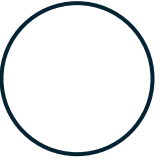
Credit: ESO/O. Furtak

# Tidal interactions

Point mass



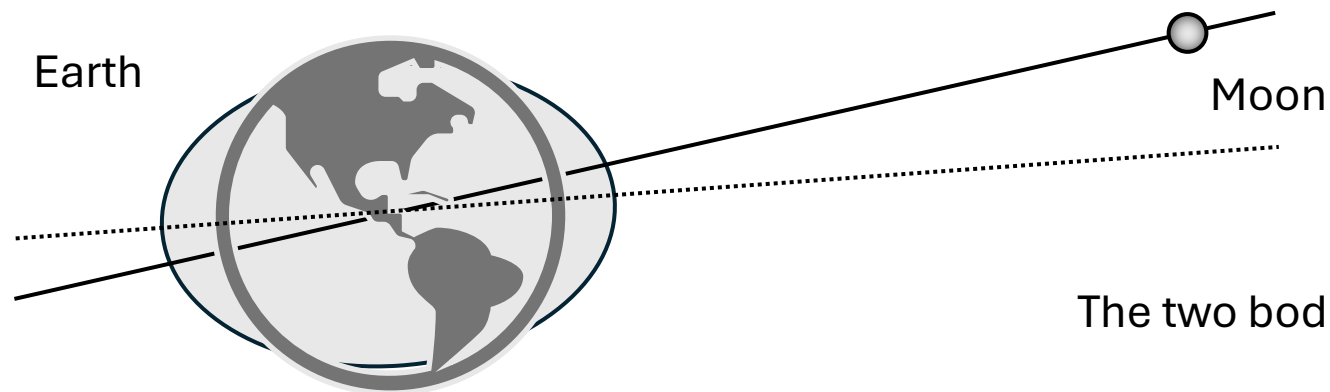
Extended body



Different points of an extended body feel **different gravitational potential**.

The body is **deformed**.

There is a **delay** between the **position of the perturber** and the **position of the tidal bulge**.

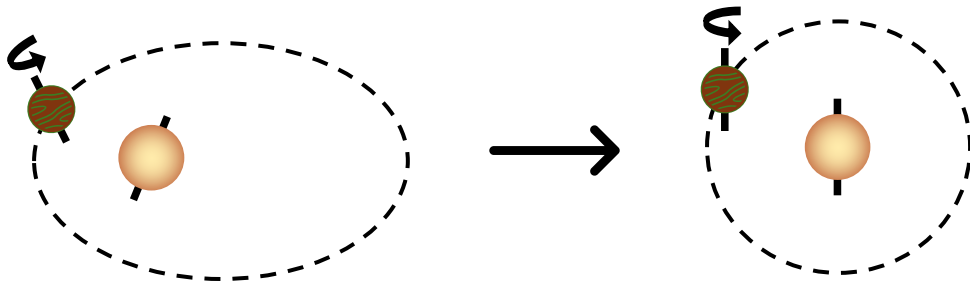


The two bodies **exchange angular momentum**.

# Tidal evolution: End state for close-in planets

One planet orbiting a star

Damping,  
Alignment,  
Synchronisation.

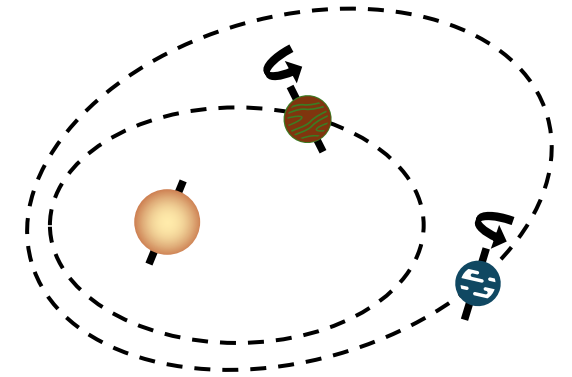


In both cases

On longer timescales, migration.

Multiple planets orbiting a star

Tidal damping and planet-planet excitation,  
Precession.



**Orbital and rotational parameters**

**evolve with time !**



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# N-body code: *Posidonius*

Blanco-Cuaresma & Bolmont, 2017

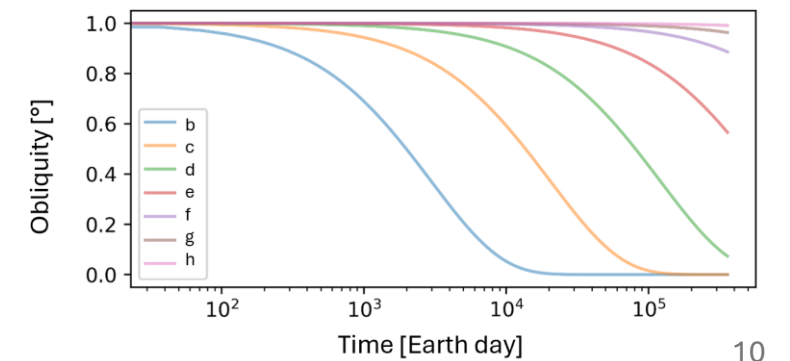
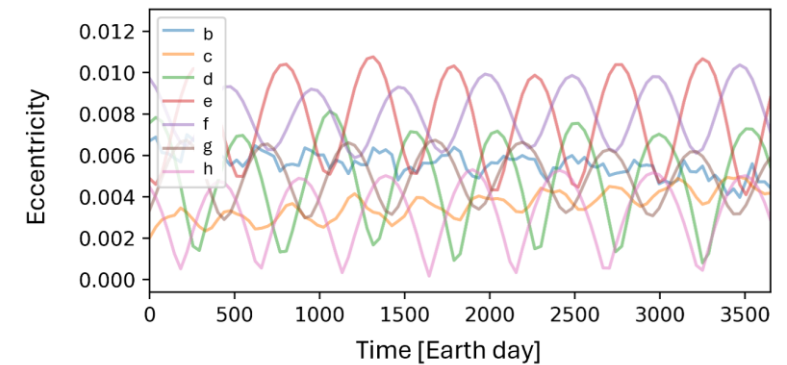
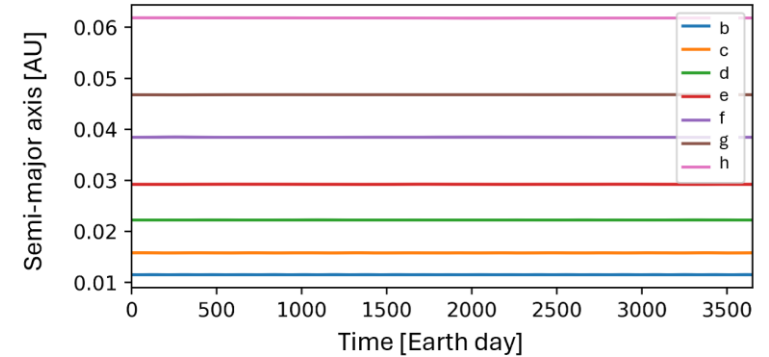
Describe the **motion** of many **interacting** particles,

Follow the **orbit** of planets, track **orbital parameters**.

Gravitation and tidal forces,

Constant time lag model.

Simulation of TRAPPIST-1 system



# Climate model

## Hierarchy of climate models

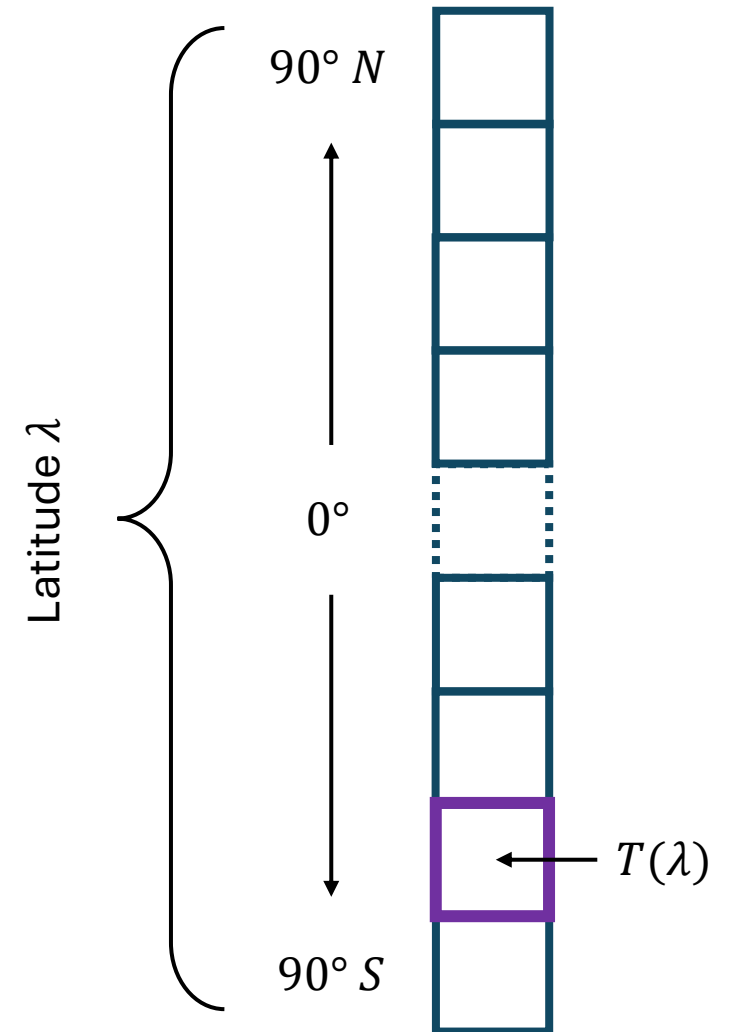
0-D Energy Balance Model (= 0-D EBM)

1-D Energy Balance Model (= 1-D EBM)

...

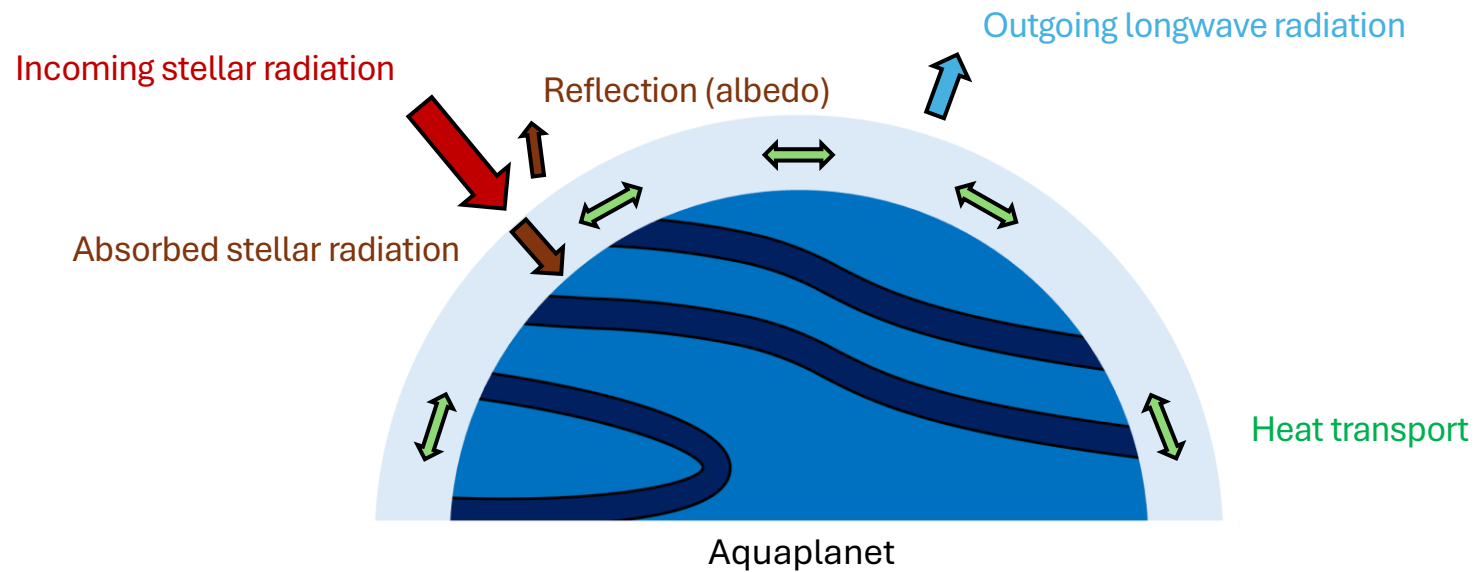
3-D Global Climate Model (= 3-D GCM)

For each **latitude**, the model computes the evolution of **temperature** with **time**.



# Radiative energy balance

- Source** of energy → Incoming stellar radiation
- Sinks** of energy → Outgoing longwave radiation
- Transport** of energy → Latitudinal heat transport

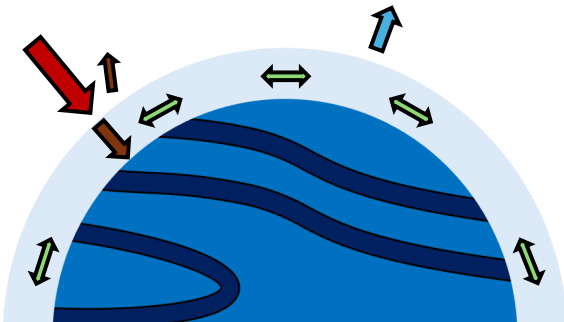


# Radiative energy balance

- Source** of energy → Incoming stellar radiation
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$$c \frac{\partial T(x, t)}{\partial t} - \frac{\partial}{\partial x} \left( D(1 - x^2) \frac{\partial T(x, t)}{\partial x} \right) + I(T) = S(1 - A(T))$$

Surface heat capacity
Heat transport
Outgoing longwave radiation
Absorbed stellar radiation

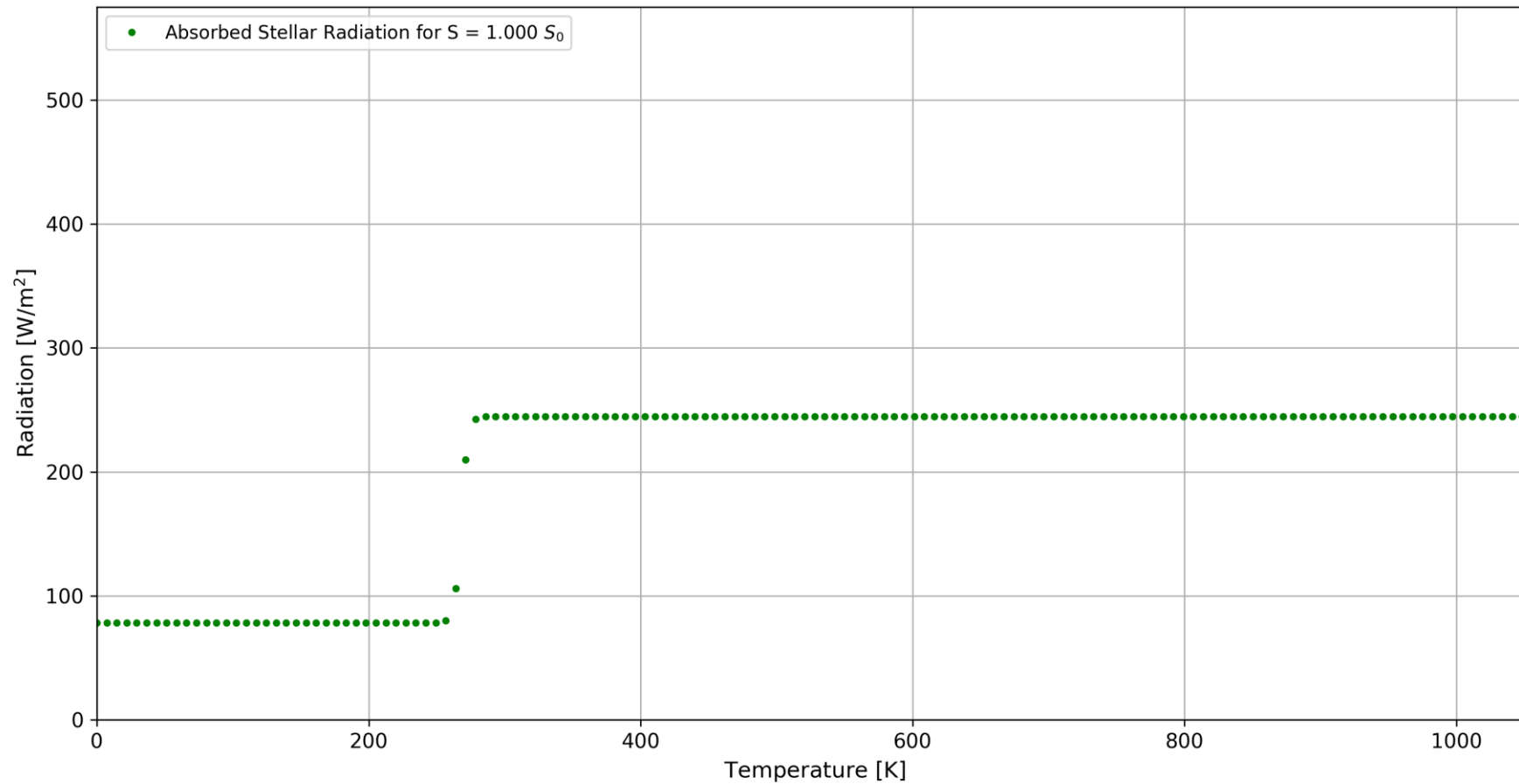


# Radiative energy balance of an Earth-like planet

$$I(T) = S(1 - A(T))$$

Absorbed stellar radiation

Amount of energy that contributes to the **heating** of the planet.

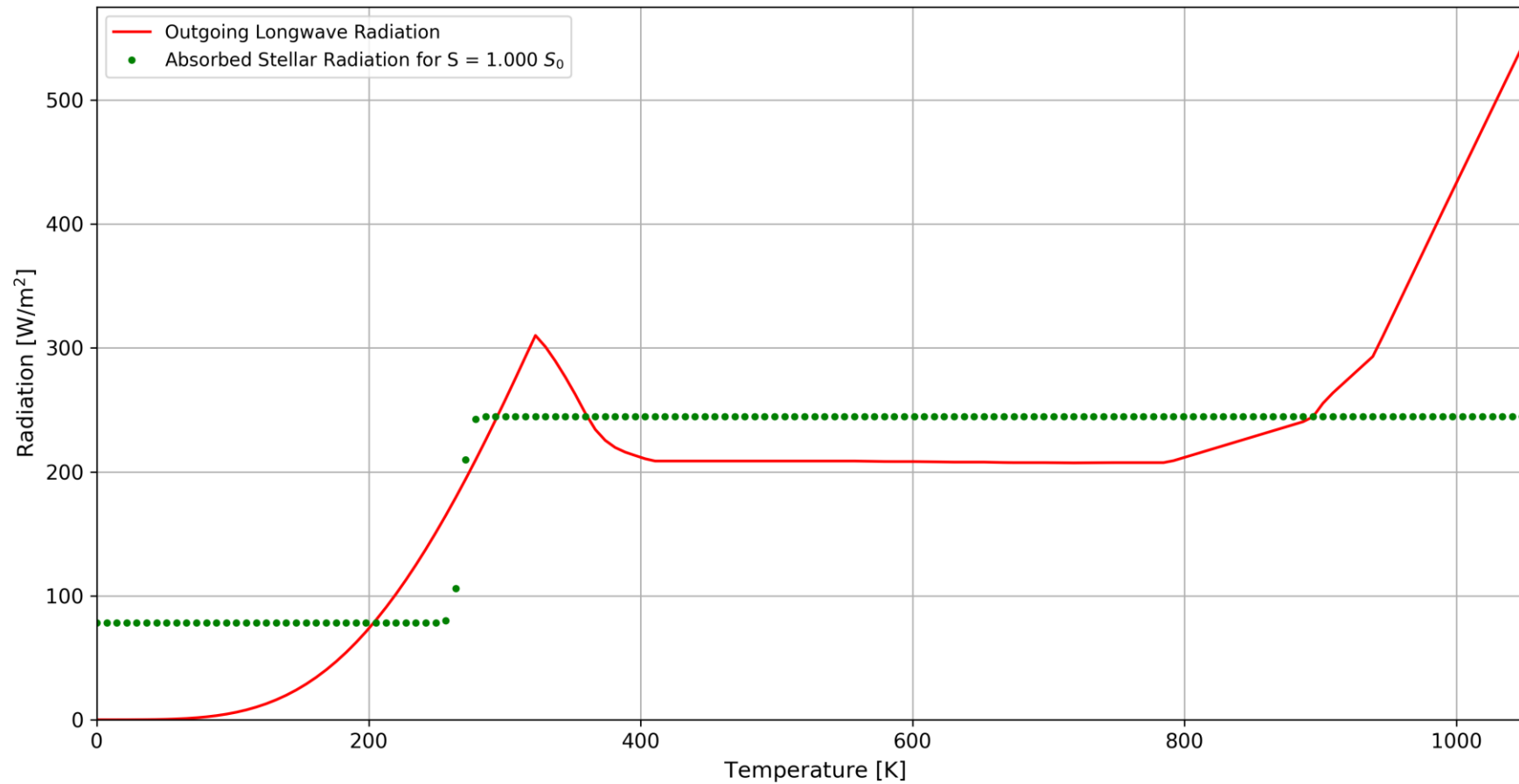


# Radiative energy balance of an Earth-like planet

$$I(T) = S(1 - A(T))$$

Outgoing longwave radiation

Amount of energy that is **radiated** away.





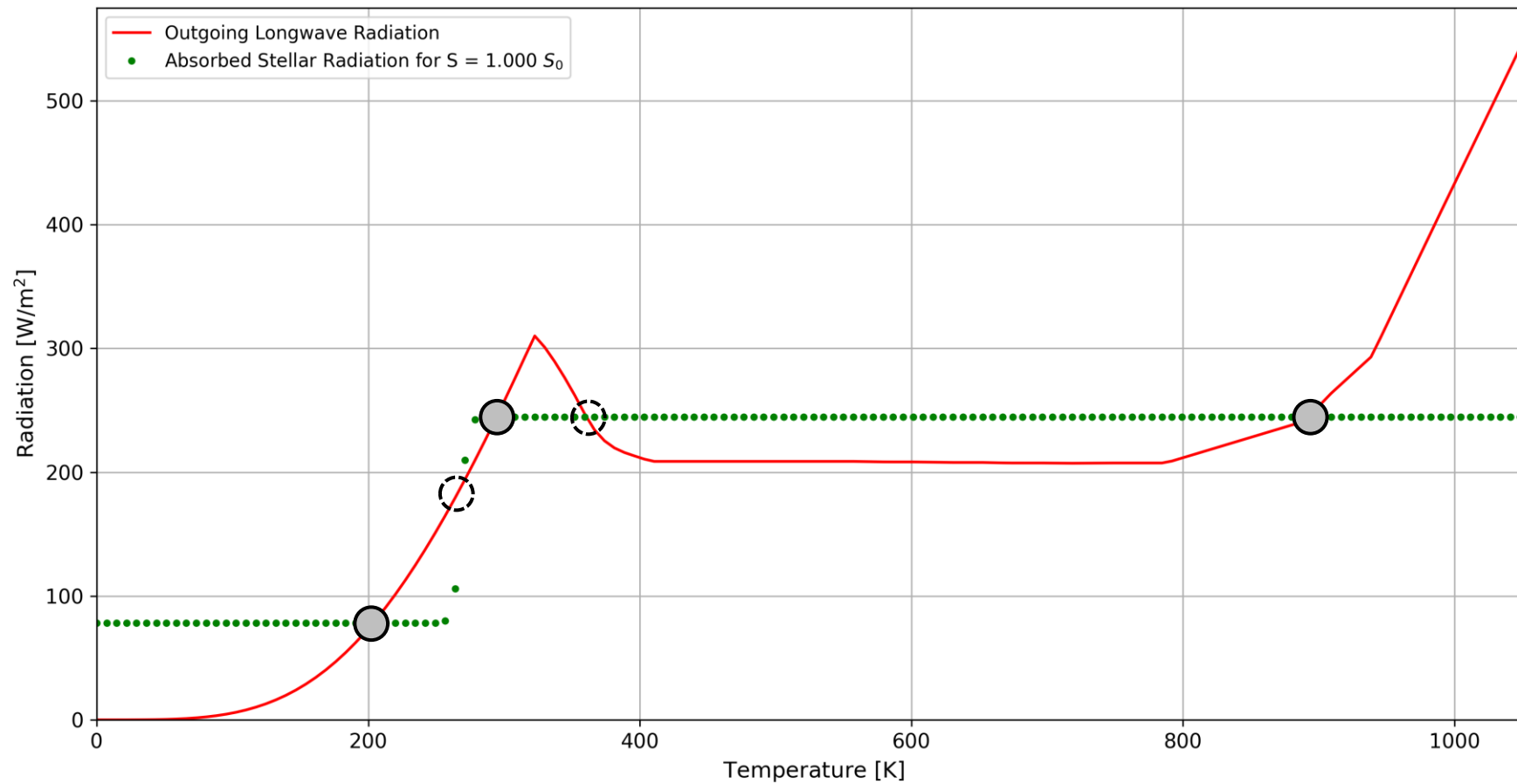
# Radiative energy balance of an Earth-like planet

$$I(T) = S(1 - A(T))$$

An **Earth-like** planet with  $S = S_0$  has :

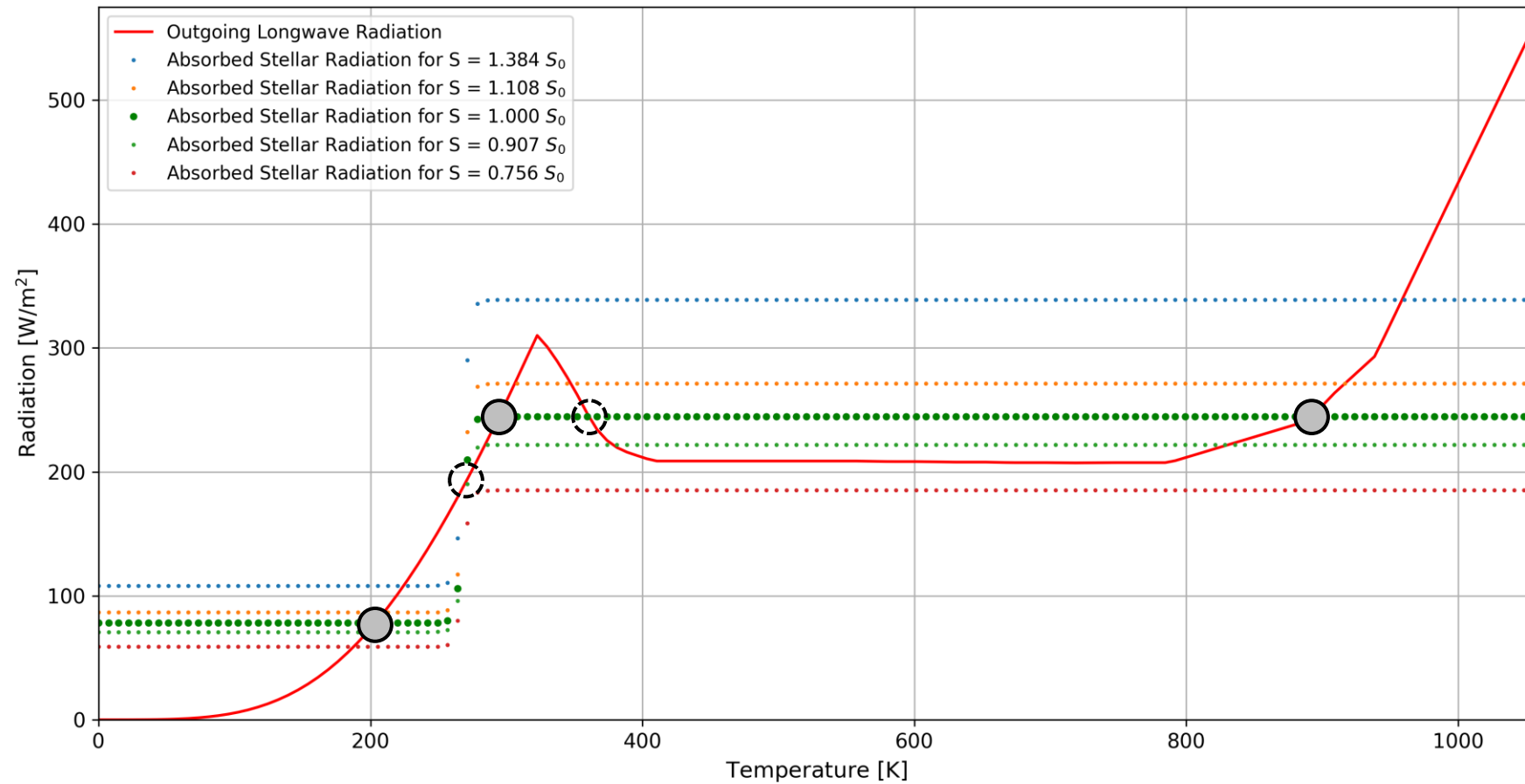
3 **stable** states     ●

2 **unstable** states     ○



# Radiative energy balance of an Earth-like planet

$$I(T) = S(1 - A(T))$$



# Feedbacks

There is an interplay between various **feedback processes**:

Boltzmann radiative feedback (**OLR**)

Ice-albedo feedback (**ASR**)

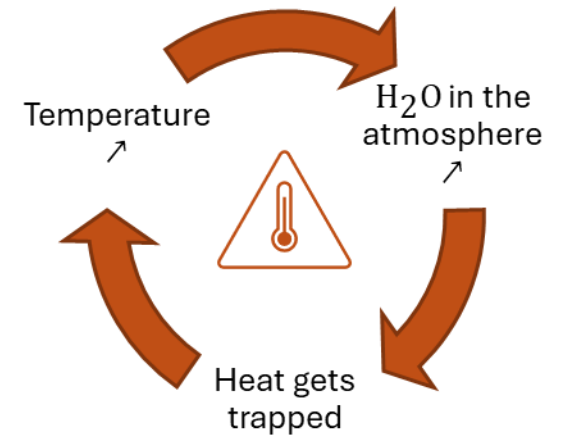
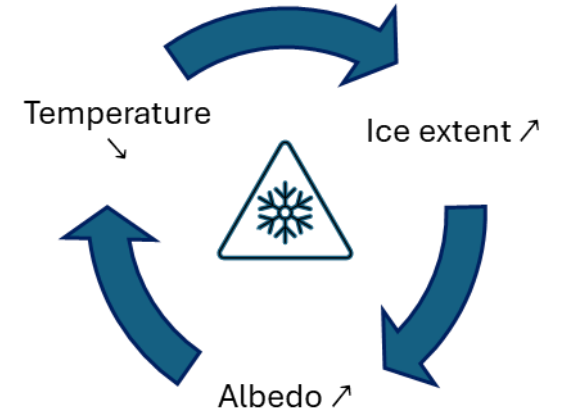
Water vapour feedback (**OLR**)

Cloud feedback (**ASR + OLR**)

Positive destabilising feedbacks →

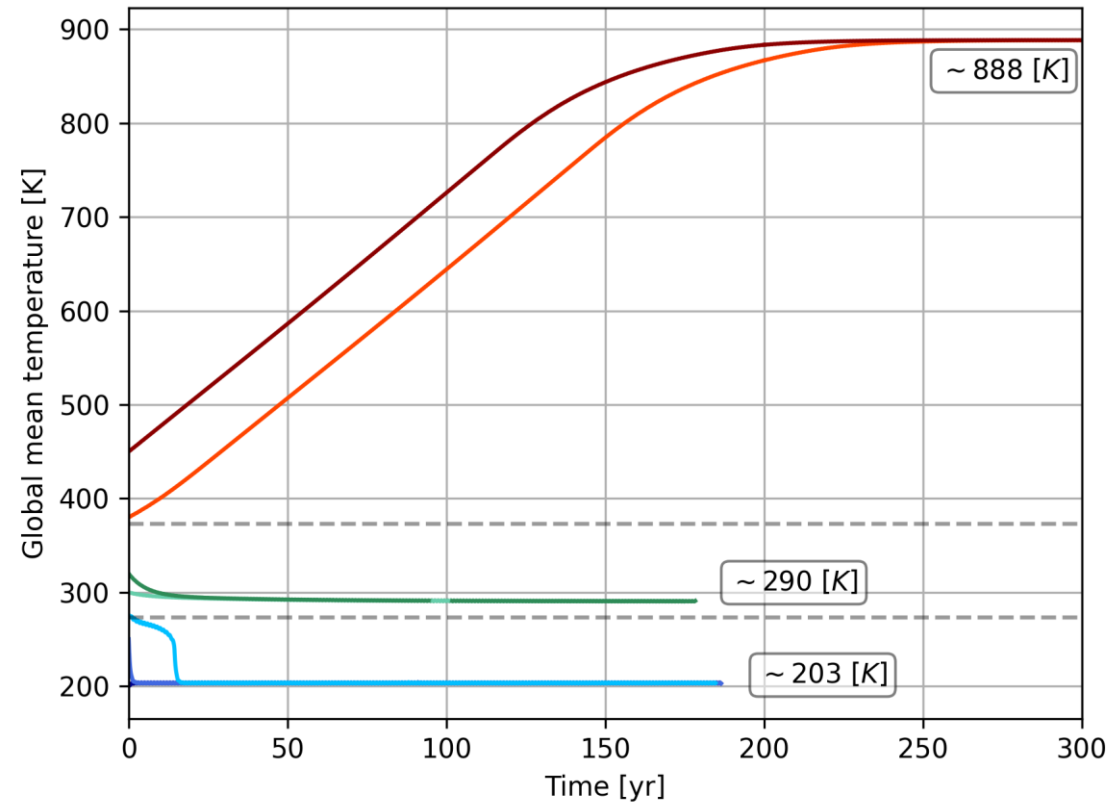
**Runaway glaciation**

**Runaway greenhouse**



# Earth-like aquaplanet

Earth-like aquaplanet  
100% ocean  
eccentricity = 0.0167  
obliquity = 23.5°



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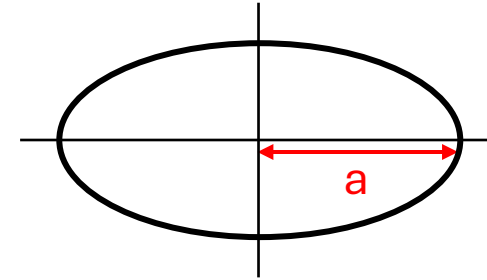
## 4. Results



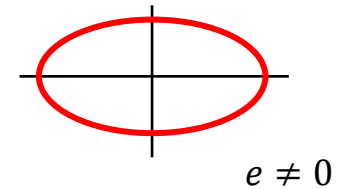
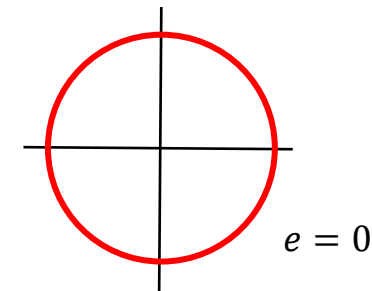
# Orbital parameters

The **daily averaged insolation** depends on orbital parameters such as:

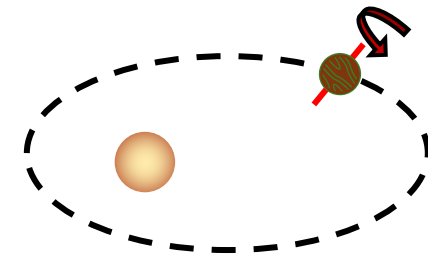
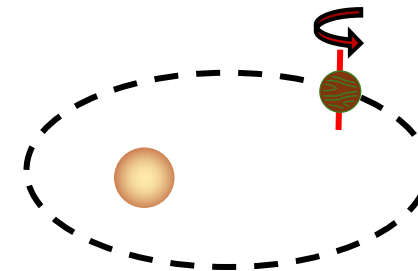
$a$  the **semi-major axis** of the planetary orbit,



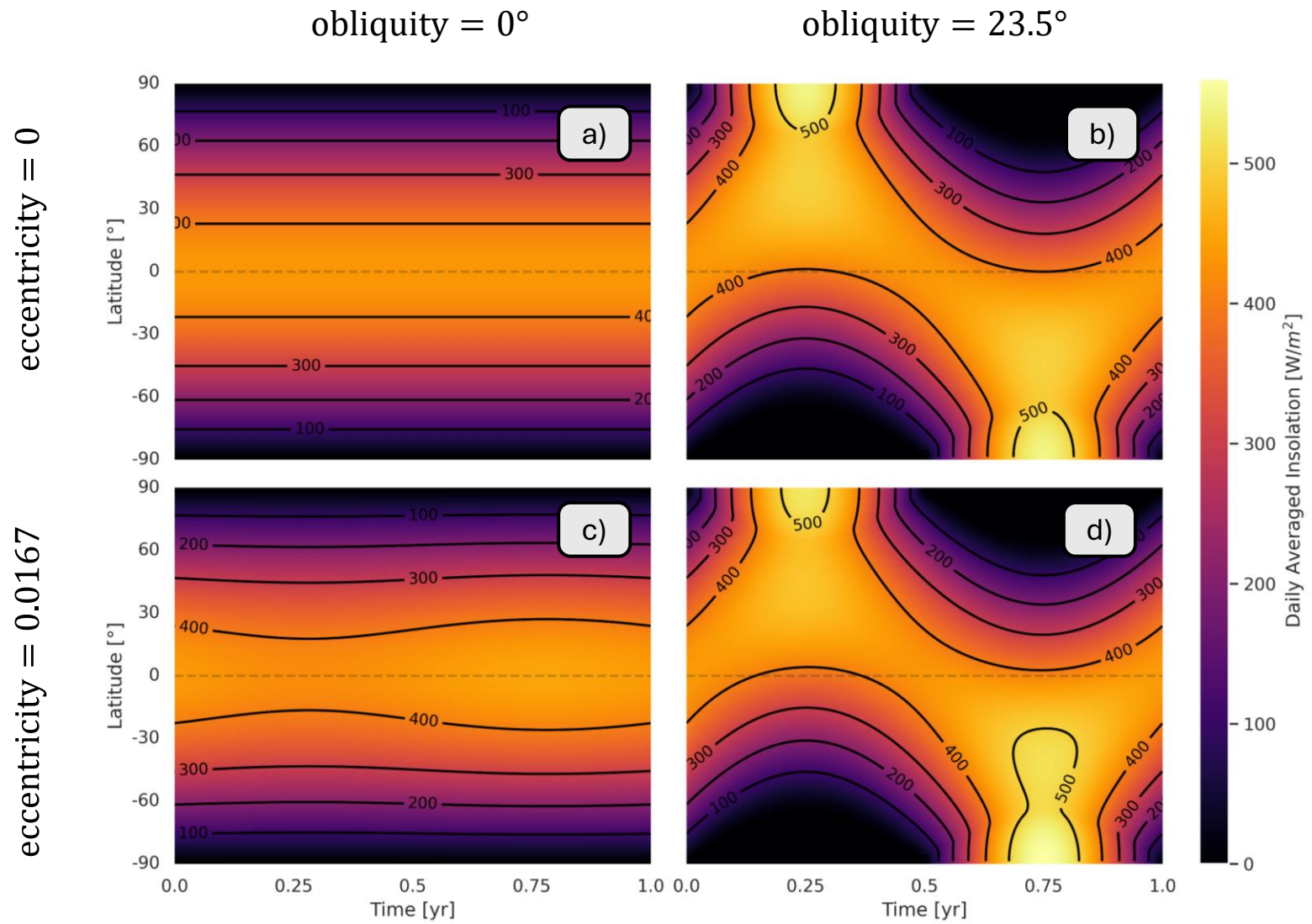
$e$  the **eccentricity** of the planetary orbit,



$\varepsilon$  the **obliquity** of the planet rotation axis.



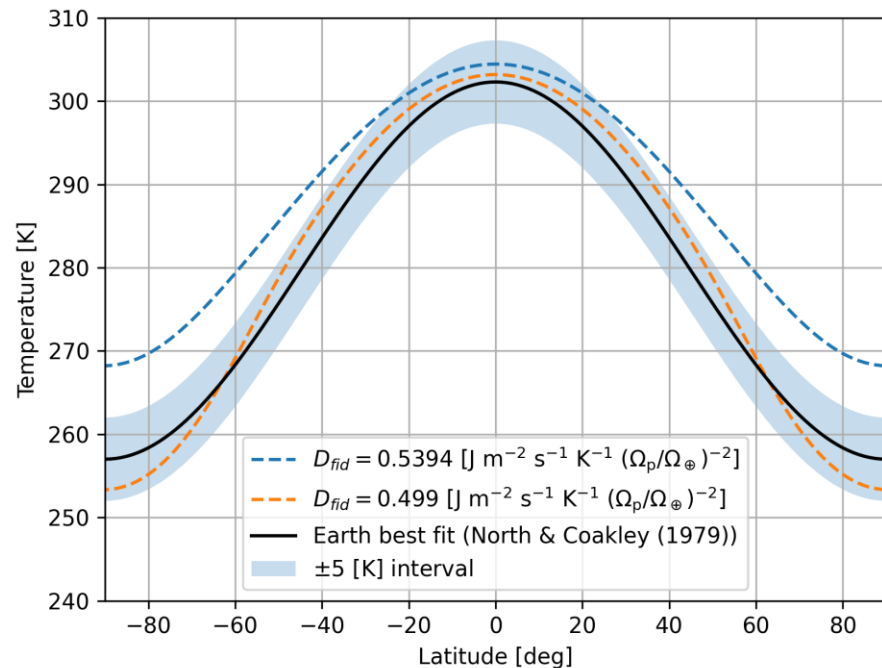
# Insolation





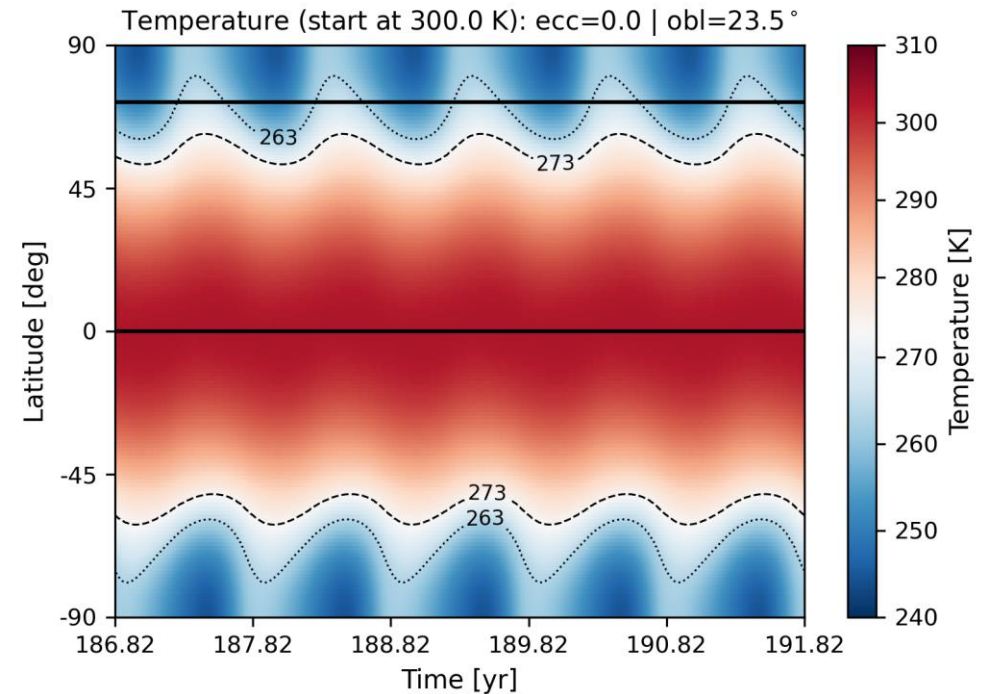
# Tuning: diffusion coefficient

Earth-like planet  
70% ocean, 30% land  
eccentricity = 0  
obliquity = 23.5°



Three criteria:

1. Global mean temperature  $294 \text{ K} \rightarrow 289 \text{ K}$
2. Mean latitudinal temperature profile
3. Mean ice line



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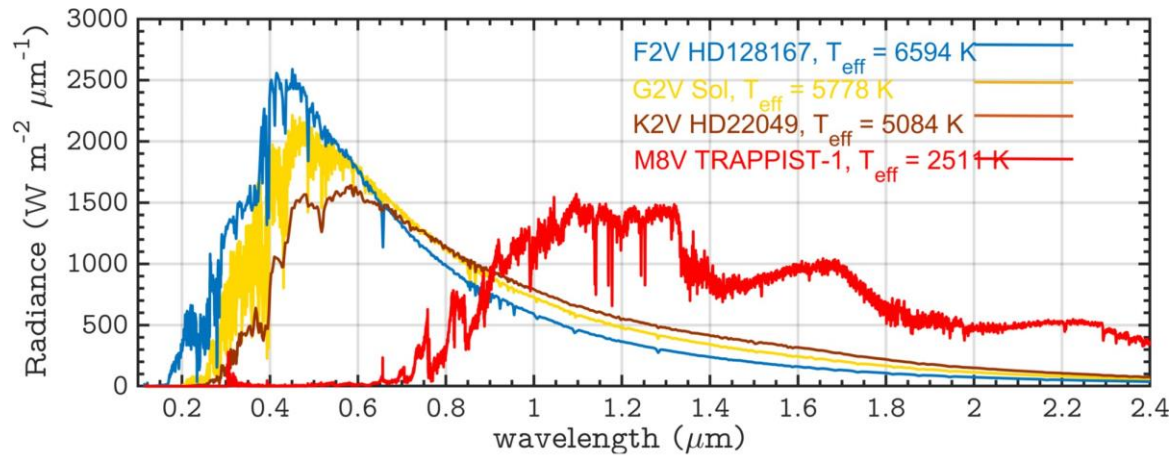
Insolation

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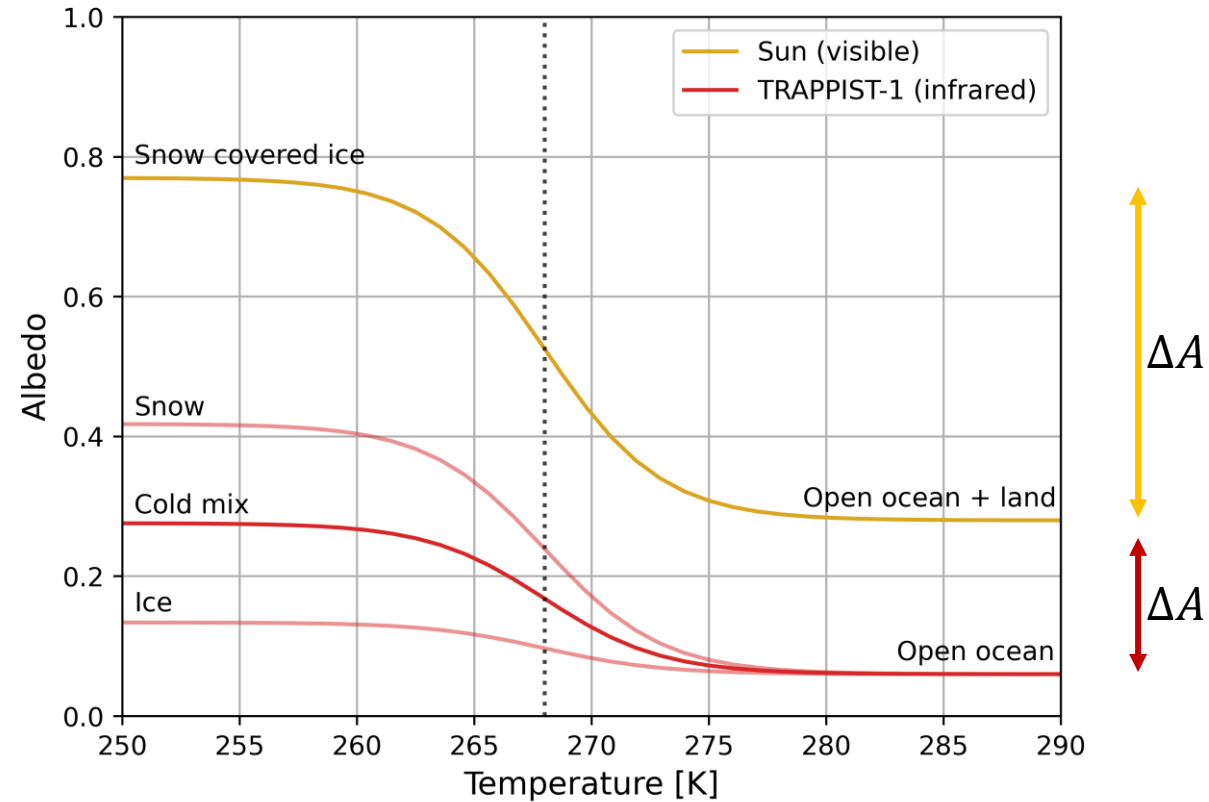
## 4. Results



# Albedo wavelength dependence

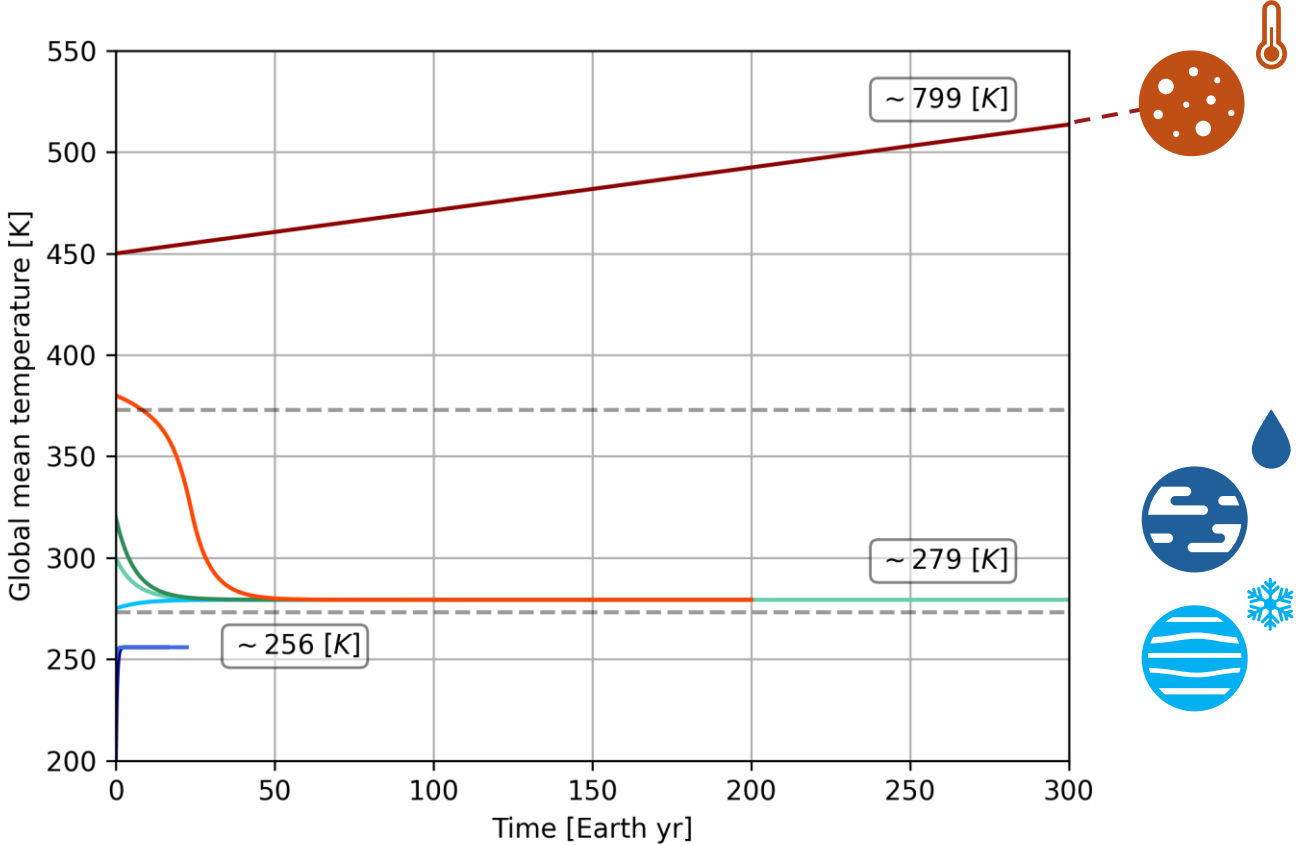


Rushby et al. 2020



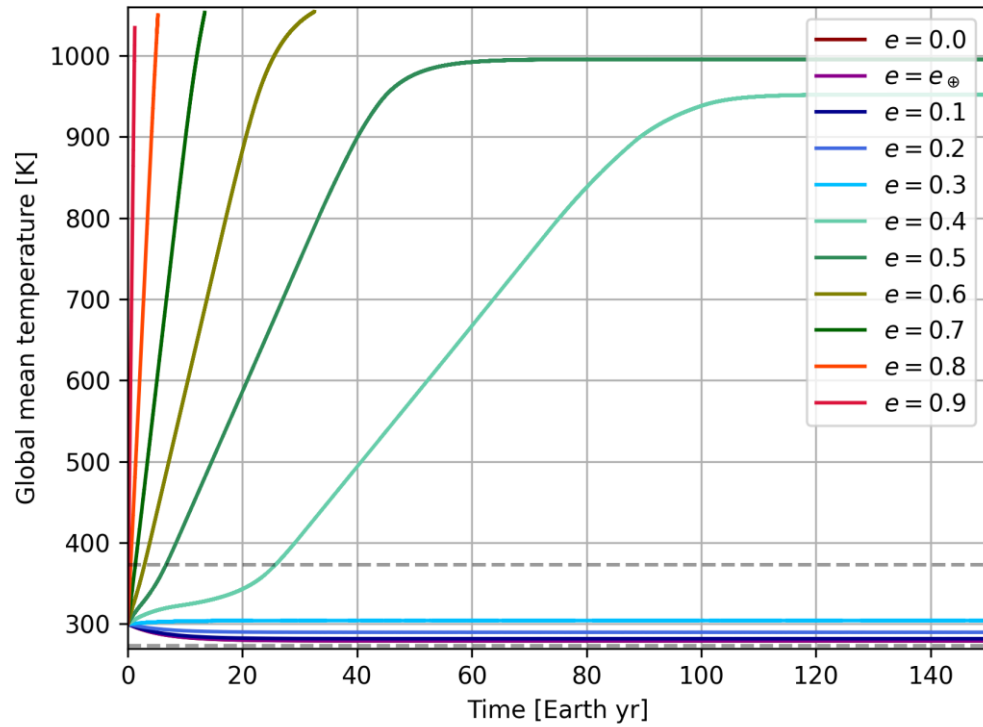
# TRAPPIST-1e

TRAPPIST-1e  
100% ocean  
eccentricity = 0  
obliquity = 0°



# Effect of constant eccentricity

TRAPPIST-1e  
100% ocean  
eccentricity =  $e_i$   
obliquity =  $0^\circ$

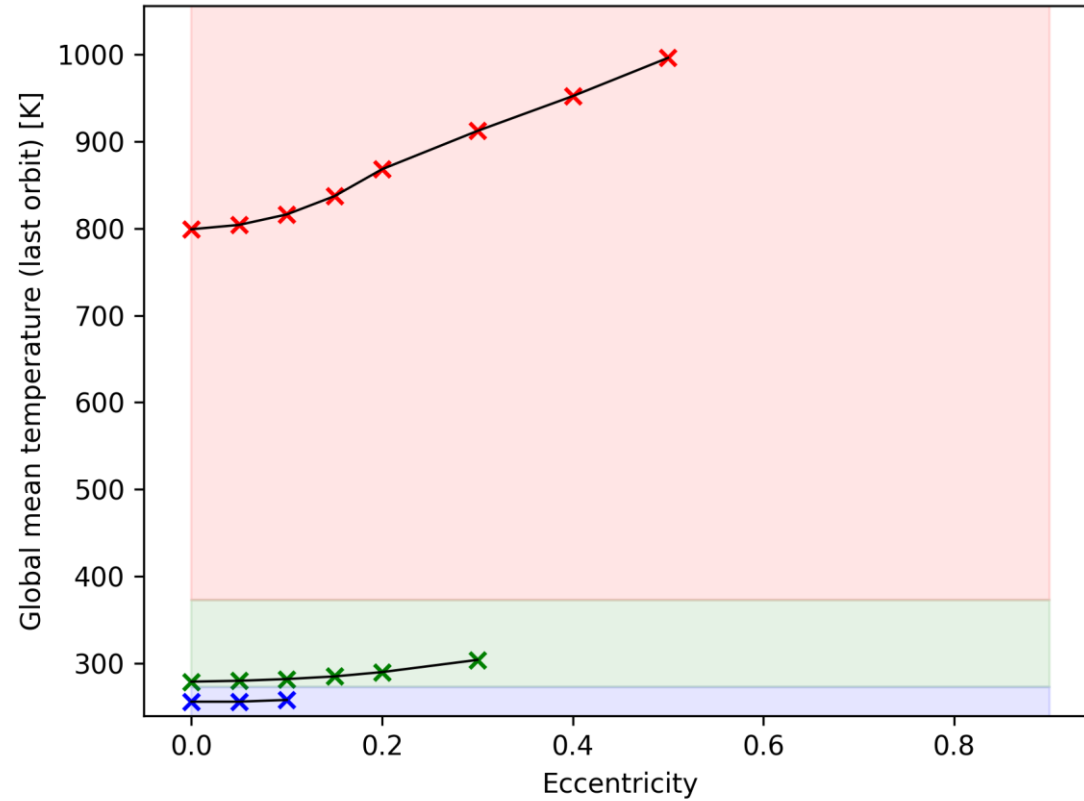


$$F = \frac{L_{star}}{4\pi a^2 \sqrt{1 - e^2}}$$

Bolmont et al. 2016

# Bifurcation diagram

TRAPPIST-1e  
100% ocean  
eccentricity =  $e_i$   
obliquity =  $0^\circ$



$T > 373 K$

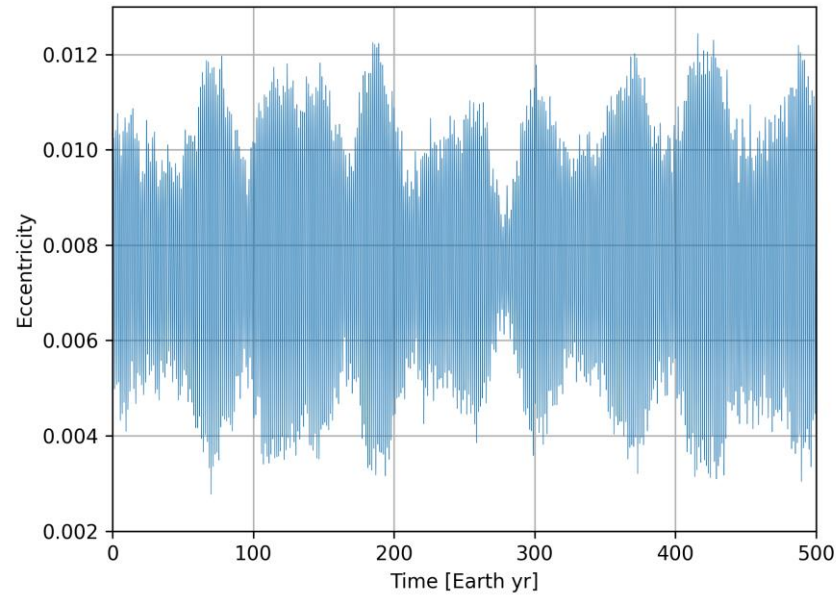
$273 K < T < 373 K$

$T < 273 K$

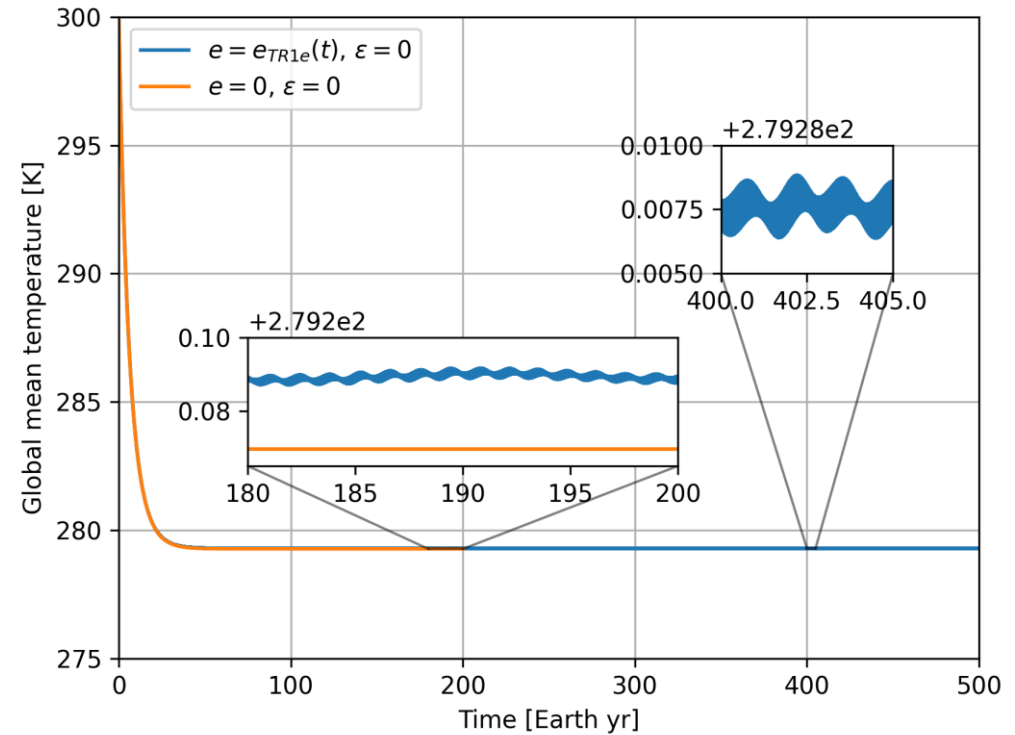
# Effect of time-dependent eccentricity

TRAPPIST-1e  
100% ocean  
eccentricity =  $\{0, e(t)\}$   
obliquity =  $0^\circ$

### N-body simulation



### Climate simulation





# Conclusion

- Slow rotating planets have a very efficient **heat transport**.
- Depending on the external forcing (eccentricity), some **stable states** become **unavailable**.
- Given observational constraints, TRAPPIST-1e would be in a **tristability** regime.
- A realistic description of the **eccentricity evolution** of TRAPPIST-1e **does not** significantly **impact** the climate.

# Outlook

- Need of observations to **constrain** our climate model.
- The EBM can be used for studies of other planetary systems (e.g. **more extreme** dynamical cases).

